Area & Perimeter

- i. Calculate the area and perimeter of a square with the following dimensions:
 - Width = 20cm

Solution: First, we'll calculate the perimeter of the square. We remember, for a square, the perimeter is given by:

 $\mathsf{Perimeter} = 4 \times \mathsf{width}$

So, in our case:

 $\mathsf{Perimeter} = 4 \times 20 = 80 \; \mathsf{cm}$

Secondly, we now want to calculate the area. We have that the area of a square is given by:

 $Area = width \times width = width^2$

So, in our case:

 $\mathsf{Area} = 20 \times 20 = 400 \ \mathrm{cm}^2$

- ii. Calculate the area and perimeter of a rectangle with the following dimensions:
 - Width = 15cm, height = 8cm

Solution: First, we'll calculate the perimeter of the rectangle. We remember, for a rectangle, the perimeter is given by:

 $\mathsf{Perimeter} = (2 \times \mathsf{width}) + (2 \times \mathsf{height})$

So, in our case:

Perimeter = $(2 \times 15) + (2 \times 8) = 30 + 16 = 46$ cm

Secondly, we want to calculate the area. We have that the area of a rectangle is given by:

 $Area = width \times height$

So, in our case:

 $\mathsf{Area} = 15 \times 8 = 120 \; \mathrm{cm}^2$

<	width >

height

width

Geometry

radius

iii. Calculate the circumference and area of a circle with the following dimensions. Leave your answers in terms of π .

- Radius = 14cm
- Diameter = 9m

Solution:

Radius = 14cm
 We remember the equations for the circumference and area of a circle:

 $\mathsf{Circumference} = 2 \times \pi \times \mathsf{radius}$

 $Area = \pi \times radius^2$

So, in our case:

 $\mathsf{Circumference} = 2 \times \pi \times 14 = 28\pi \mathsf{ cm}$

Area =
$$\pi \times 14^2 = 196\pi \text{ cm}^2$$

• Diameter = 9m

We have the equations above for the circumference and area of a circle but they are in terms of a radius. We must convert them first. We remember:

 $\mathsf{diameter} = 2 \times \mathsf{radius}$

So, we have the equivalent equations in terms of a diameter:

 $\mathsf{Circumference} = \pi \times \mathsf{ diameter}$

Area = $\pi \times \left(\frac{\text{diameter}}{2}\right)^2$

So, in our case:

$${\rm Circumference}=\pi\times9=9\pi~{\rm m}$$

Area
$$= \pi imes \left(rac{9}{2}
ight)^2 = 20.25\pi$$
 m²

NOTE: If we have a semi-circle, then the area and circumference can be computed as above, but you must remember to half the result.

- iv. Calculate the area of the right angle triangle with the following dimensions:
 - Height = 12cm, Width=7cm

Solution: We remember, for a rectangle, the area is given by:

$$Area = width \times height$$

So, in the case of a right-angle triangle, which is a rectangle cut in half diagonally, the area is given by:

$$\mathsf{Area} = \frac{\mathsf{width} \times \mathsf{height}}{2}$$

Hence, for our right angle triangle, we find that:

$${\rm Area} = \frac{7 \times 12}{2} = \frac{84}{2} = 42 \ {\rm cm}^2$$

v. Calculate the perimeter of a regular octagon with vertices of 5cm

Solution: We remember, for any regular polygon, the perimeter is given by

 $Perimeter = Length of Vertices \times Number of Vertices$

So, for an octagon, with 8 sides of 5cm each, we obtain:

 $\mathsf{Perimeter} = 5 \times 8 = 40 \; \mathsf{cm}$

